

Background

- PhD student at the division of Signals and Systems at Uppsala university
- Joined SEDDIT in 2025



Sensor informatics and Decision-making
for the Digital Transformation



UPPSALA
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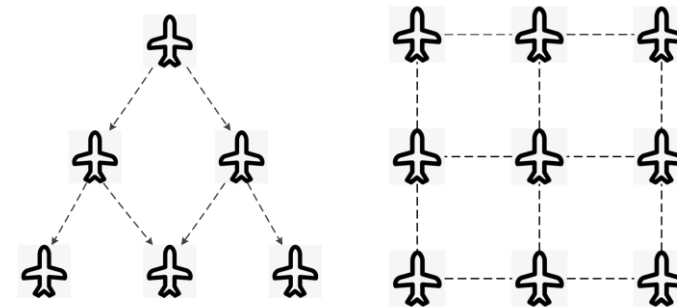
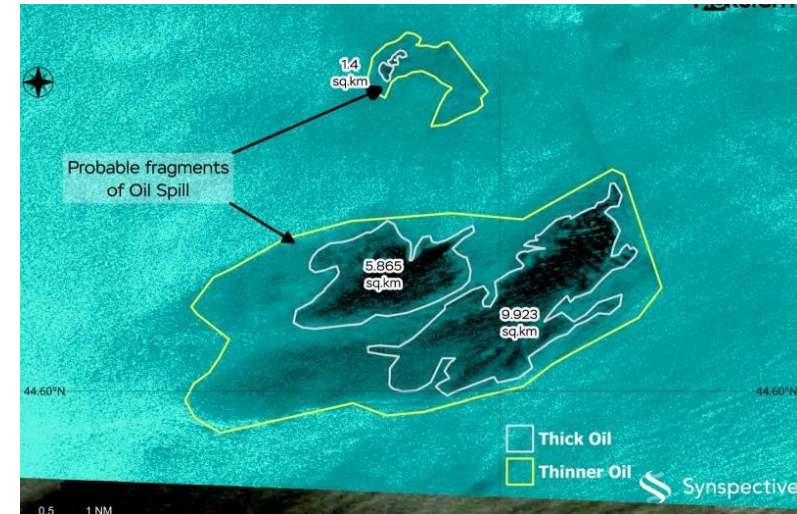
Project motivation

- Develop algorithms for collaborative autonomous multi-agent systems
- Applications
 - Search & rescue
 - Environmental monitoring
- Tasks
 - Explore, locate, track, transport, monitor
- **Challenges**
 - Distributed setting (no 'global' information)
 - Uncertain environments
 - Unreliable and limited communication
 - Need to simultaneously perform task and learn from the environment



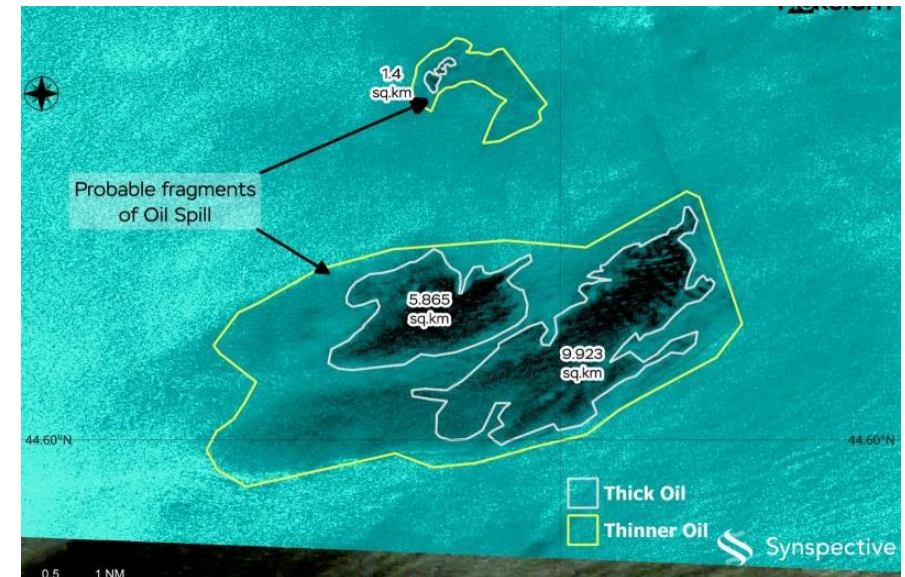
Research areas

- We aim to address these challenges by combining
 - Multi-agent control theory
 - Collaborative reinforcement learning
 - Decentralized sensor fusion
- Formation control applications
 - monitoring of environmental boundaries
 - coordinated detection and tracking
- Standard formations
 - Fixed (pre-specified) shape
 - Distance or bearing constraints
 - Rigid formations



Multi-agent formation control

- Many naturally occurring phenomena are dynamic (deformable), irregular, and continuous
 - Better described by parametric curves rather than fixed geometric shapes
- In target enclosing tasks, forming a smooth, adaptive boundary around a point of interest is often sufficient
- **Current work:** flexible formation control
- Instead of specifying exact locations of each agent, control the formation shape indirectly by specifying
 - Location (center)
 - General shape (“frequency content”)

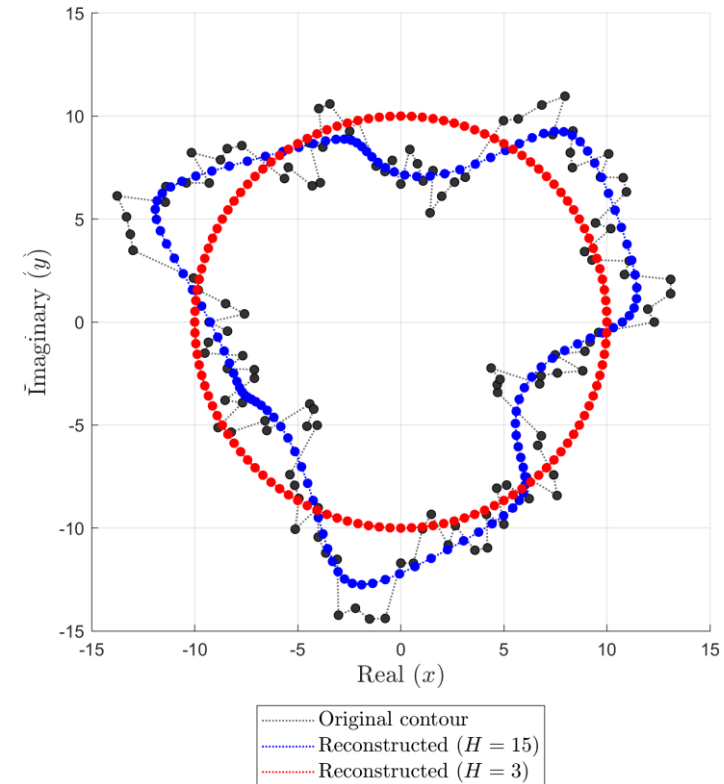


Frequency domain descriptions of shapes

- Closed curves can be seen as a superposition of a series of elliptical curves with increasing frequency

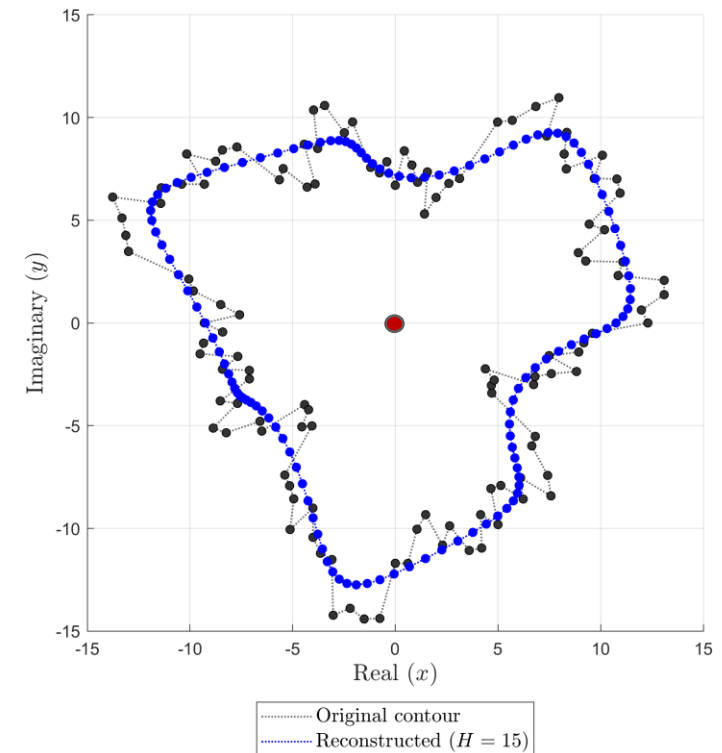
$$\begin{bmatrix} x(t) \\ y(t) \end{bmatrix} = \begin{bmatrix} a_0 \\ c_0 \end{bmatrix} + \sum_{k=1}^{\infty} \begin{bmatrix} a_k & b_k \\ c_k & s_k \end{bmatrix} \begin{bmatrix} \cos kt \\ \sin kt \end{bmatrix}$$

- Low frequency \rightarrow "global" shape
- High frequency \rightarrow details
- A convenient encoding of such shapes is given by Fourier descriptors (FDs)
- FDs are the coefficients of the discrete Fourier transform (DFT)
- Convenient separation of centroid and shape



Related work

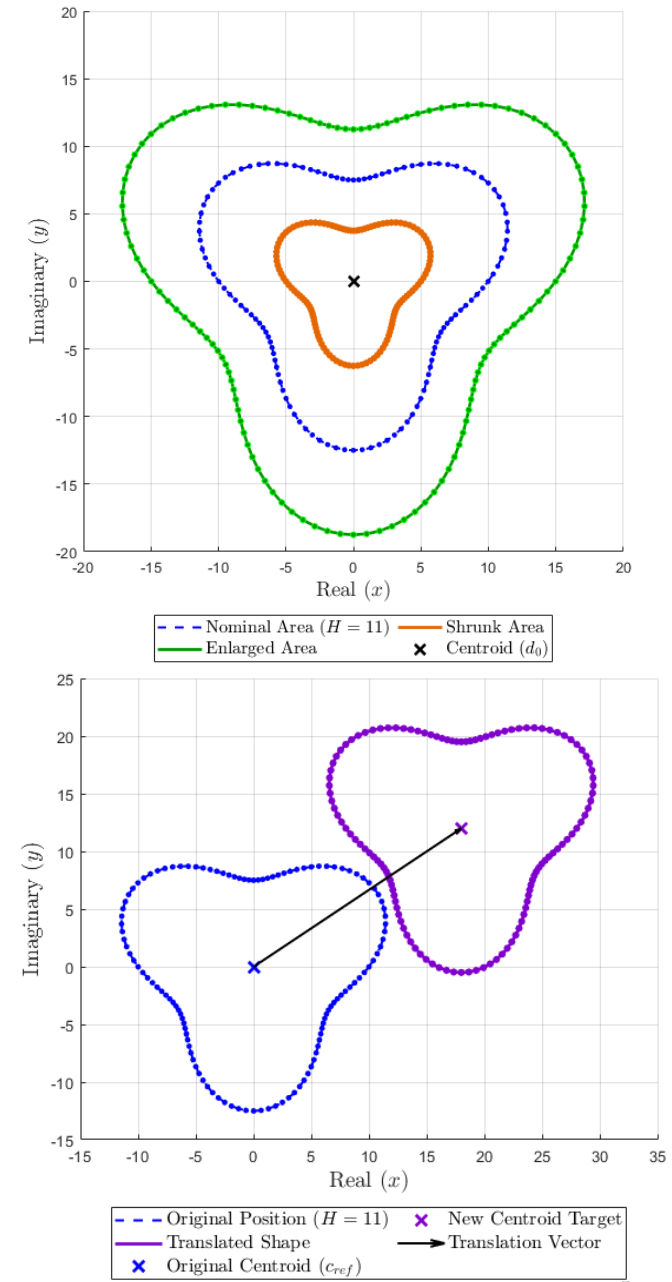
- Recent works exploit Fourier descriptors to
 - track evolving irregular boundaries
 - implicitly defining formation shapes
 - agents form an ellipse from any given initial conditions
 - “emergent formations”
- There also exists algorithms for
 - Distributed estimation of FDs
 - Control laws such that agents form formations with a certain low-frequency content (shapes with a certain selected set of non-zero FDs)
- **Problems:**
 - Fixed formation **centroid** (determined by initial conditions)
 - Non-increasing **scale** (can lead to shrinking/flat formations)



Recent work

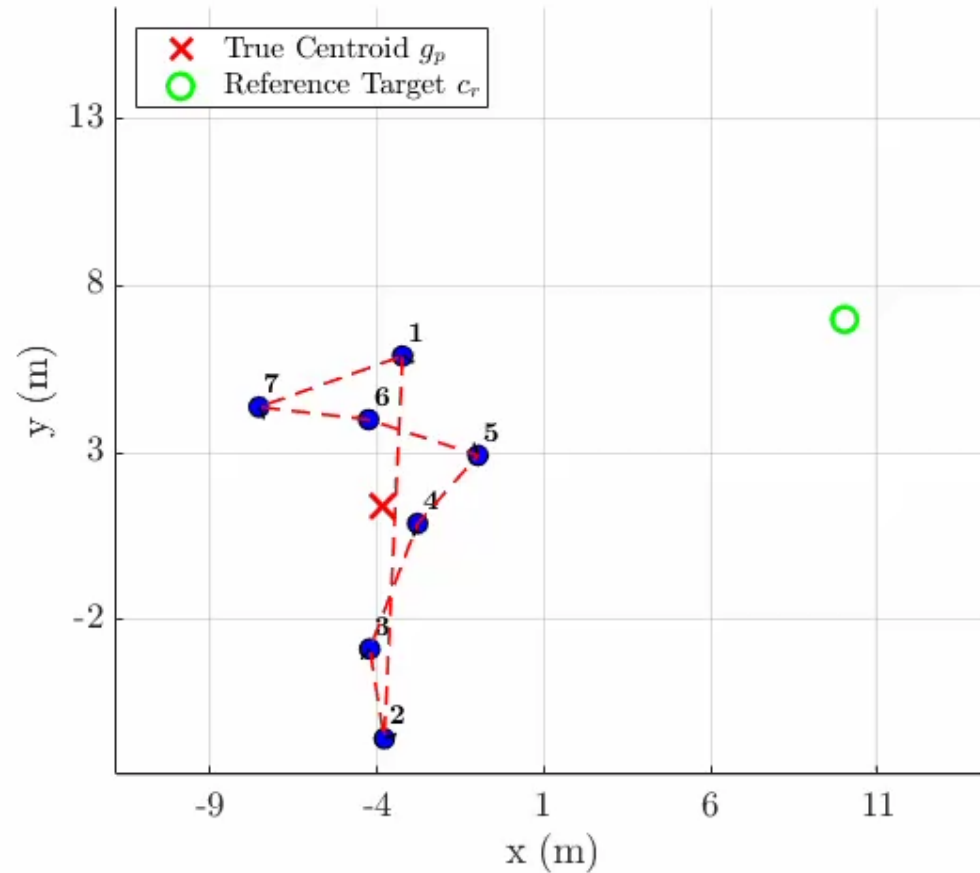
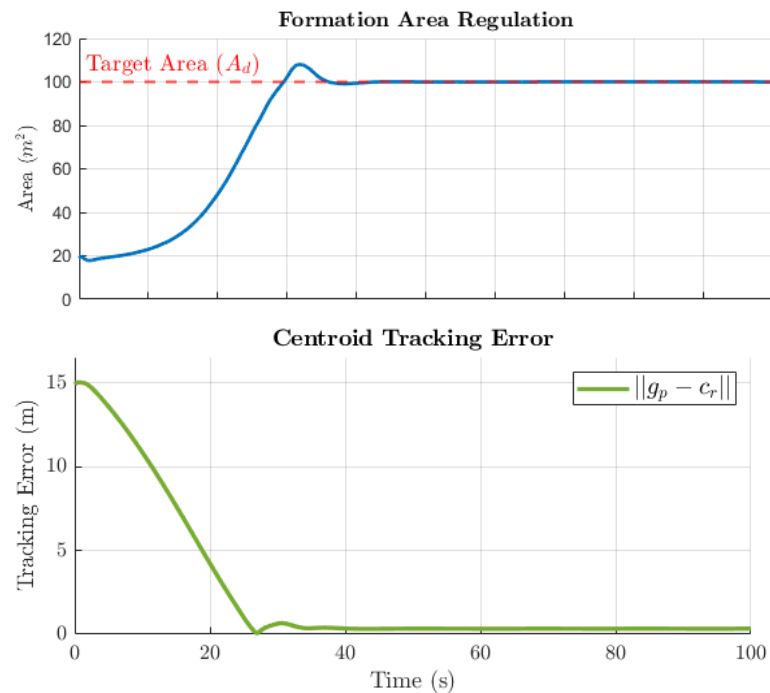
- In a recent paper, we address the scale and centroid limitations by introducing:
 - Area regulation
 - Centroid tracking
- Interesting for high-level tasks:
 - "Distribute around a point and track it"
 - Agent's automatically form a shape that 'works'
 - Any formation shape with a certain
 1. low-frequency content
 2. centroid
 3. enclosed area

is valid
- Distributed setting:
 - each agent only needs to know its own position and orientation + local communication (neighbour-to-neighbour)



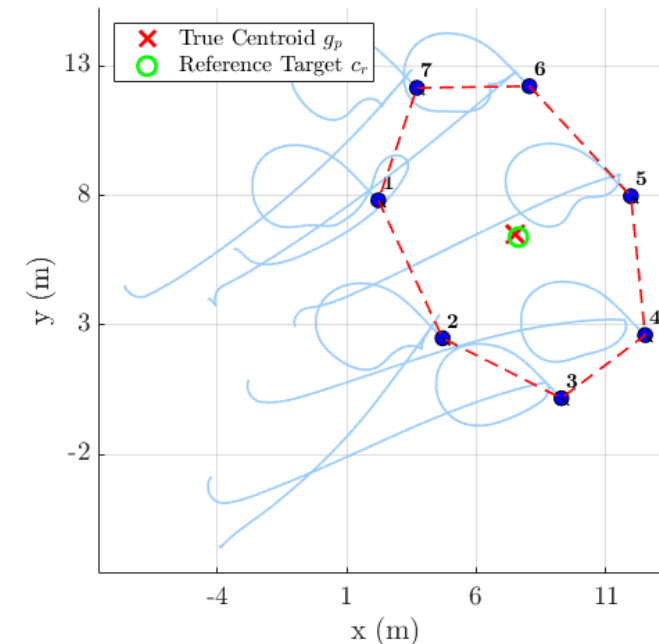
Simulations

- 7 unicycle agents in random initial locations
 - Convergence to an elliptical shape
 - Convergence to a desired enclosed area
 - Centroid tracking



Conclusion and future work

- We have developed a distributed control strategy for multi-agent formations.
- By leveraging properties of Fourier descriptors, the proposed framework allows agents to
 - form and maintain formations with a prescribed enclosed area
 - track a desired average position.
- Future work will focus on
 - Control of other geometric characteristics (shape orientation)
 - Higher-order systems (more complex agent dynamics)
 - Uncertainties in position/orientation



Thank you!

- Questions?

